# UNIVERSITY OF TLEMCEN FACULTY OF SCIENCES DEPARTMENT OF PHYSICS <br> <br> $1^{\text {st }}$ YEAR L M D SM \& ST <br> <br> $1^{\text {st }}$ YEAR L M D SM \& ST <br> <br> $\boldsymbol{P}_{\text {Ractical }}$ Work $^{\text {a }}$ <br> <br> $\boldsymbol{P}_{\text {Ractical }}$ Work $^{\text {a }}$ OF OF <br> <br> PHYSICS (MECHANICS) <br> <br> PHYSICS (MECHANICS) <br>  

## GENERAL RECOMMENDATIONS

## 1- ORGANISATION :

- A physics (mechanics) practical work PW is scheduled once a fortnight for each group.
- The practical works are performed in ascending order. Example: a student who does PW n ${ }^{\circ} 3$ in the first session will do PW $n^{\circ} 4$ in the following session.
- Any justified absence will be made up for in a catch-up session scheduled by the same teacher.
- The justification must be approved by the vice-dean of pedagogy within 48 hours following the absence.
-In case of delay in submitting the justification to the responsible of the matter (more than a week after the absence), the student will have a zero.
- Any unjustified absence will be penalized with a zero.


## 2- DISCIPLINE IN THE LABORATORY:

A student who comes to physics laboratory must:

- Behaves as a respectful and conscientious student.
- Comes on time (no delay) to the practical session.
- Puts on a white apron.
- Stores stools under benches before going out.
- Has prepared his manipulations (students will be questioned and marked accordingly).
- Brings a scientific calculator and the necessary equipment to draw graphs (pencil, eraser, 30 cm ruler, millimeter sheets, etc.), no exchange of equipment (calculator, pencils, etc.) between students will be tolerated.
- The use of the mobile phone is strictly prohibited even to use it as a calculator.


## 3- REPORTS:

- The practical work session is reserved for the manipulation and exploitation of the results.
- The curves must be drawn in pencil on an entire graph sheet (millimeter paper).
- Reports should be :
a- Written, properly, on practical work sheets provided by the teacher.
b- Given individually to the teacher at the end of the session.
- The marks will be provided to students by the responsible teachers fifteen (15) days after the submission of the reports.


## List of physical quantities

The mass = La masse $=\boldsymbol{m}$
The length $=$ La longueur $=\boldsymbol{l}$
The distance $=$ La distance $=\boldsymbol{d}$

The time = Le temps $=\boldsymbol{t}$
The stiffness constant $=$ La constante de raideur $=\boldsymbol{k}$
The period = La période $=\boldsymbol{T}$

The speed $=$ La vitesse $=\boldsymbol{v}$

The accélération $=$ L'accélération $=\boldsymbol{a}$

The earth's gravitaional accélération = L'accélération gravitaionnelle terrestre = g
The angle of inclination = l'angle d'inclinaison $=\boldsymbol{\theta}$
The coefficient of dynamic friction $=$ Le coefficient de frottement dynamique $=\boldsymbol{\mu}_{\boldsymbol{d}}$
The coefficient of static friction $=$ Le coefficient de frottement statique $=\boldsymbol{\mu}_{\boldsymbol{s}}$
Height $=$ hauteur $=\boldsymbol{h}$

## Used material

A carriage $=$ Un chariot
A millimeter sheet $=$ Une feuille millimétrée

A spring = Un ressort
A digital stopatch $=$ Un chronomètre digital
Optical forks = Des fourches optiques

A gratuated ruler = Une règle graduée
Felt $=$ feutrine
Free fall = Chute libre
A road = Une tige
Mini launcher $=$ Mini lanceur
A pendulum $=$ Un pendule
A wire $=$ Un fil $\quad$ A protractor $=$ Un rapporteur

## INTRODUCTION TO PHYSICS PRACTICAL WORK

## REMINDER ON THE LINEAR REGRESSION METHOD

We use the linear regression method only when the absolute uncertainty on $\boldsymbol{x}$ is negligible ( $\Delta \boldsymbol{x} \approx$ $\mathbf{0}$ ) and the absolute uncertainty on $\boldsymbol{y}$ is constant ( $\Delta \boldsymbol{y}=\boldsymbol{c s t e}$ ).
This method consists in drawing the best possible straight line of equation $\boldsymbol{y}=\boldsymbol{a}+\boldsymbol{b} \boldsymbol{x}$ which passes as close as possible to all the experimental points, as illustrated in figure 1.
$\boldsymbol{b}$ represents the slope of the regression line while $\boldsymbol{a}$ is the ordinate at the origin.


Figure 1

Knowing that we have $\boldsymbol{n}$ measurements performed in practical work, then the values of $\boldsymbol{a}$ and $\boldsymbol{b}$ are given by the formulas:

$$
\begin{align*}
& a=\frac{\sum_{i=1}^{n} x_{i}^{2} \sum_{i=1}^{n} y_{i}-\sum_{i=1}^{n} x_{i} y_{i} \sum_{i=1}^{n} x_{i}}{D_{x}}  \tag{1}\\
& b=\frac{n \sum_{i=1}^{n} x_{i} y_{i}-\sum_{i=1}^{n} x_{i} \sum_{i=1}^{n} y_{i}}{D_{x}}  \tag{2}\\
& D_{x}=n \sum_{i=1}^{n} x_{i}^{2}-\left(\sum_{i=1}^{n} x_{i}\right)^{2} \tag{3}
\end{align*}
$$

The uncertainties associated with each parameter are given by:

$$
\begin{align*}
& \Delta y=\sqrt{\frac{1}{n-2} \sum_{i=1}^{n}\left(y_{i}-\left(a+b x_{i}\right)\right)^{2}}  \tag{4}\\
& \Delta a=\Delta y \sqrt{\frac{\sum_{i=1}^{n} x_{i}^{2}}{D_{x}}}  \tag{5}\\
& \Delta b=\Delta y \sqrt{\frac{n}{D_{x}}} \tag{6}
\end{align*}
$$

If the linear regression line passes through the origin, we have the equation of the line $\boldsymbol{y}=\boldsymbol{b} \boldsymbol{x}$, in this case $\boldsymbol{a}=\mathbf{0}$ and we obtain:

$$
\begin{align*}
& b=\frac{\sum_{i=1}^{n} x_{i} y_{i}}{\sum_{i=1}^{n} x_{i}^{2}}  \tag{7}\\
& \Delta y=\sqrt{\frac{1}{n-1} \sum_{i=1}^{n}\left(y_{i}-b x_{i}\right)^{2}}  \tag{8}\\
& \Delta b=\frac{\Delta y}{\sqrt{\sum_{i=1}^{n} x_{i}^{2}}} \tag{9}
\end{align*}
$$

Family \& First names :
Date of Birth :
Group :
Date : Laboratory $\mathrm{n}^{\circ}$ :

## Corrector :

Mark :

## PW 1: INTRODUCTION TO PHYSICS PRACTICAL WORK

Experience : A scale repairer wants to replace a defective spring in a scale. The spring must have a stiffness constant $\boldsymbol{k}=(\mathbf{3 . 0 0} \pm \mathbf{0 . 0 5}) \boldsymbol{N} / \boldsymbol{m}$ and a negligible mass. In his workshop, he found a spring of negligible mass but its stiffness constant is unknown.

Using Hook's Law : $\boldsymbol{F}=\boldsymbol{k} \times \boldsymbol{d}$, where $\boldsymbol{F}$ represents the force applied to the spring, $\boldsymbol{k}$ the stiffness constant and $\boldsymbol{d}$ the elongation, he was able to calculate the value of $\boldsymbol{k}$. As a result, he hung different masses on the spring and measured its elongation. Hook's law simplifies to :

$$
\begin{equation*}
d=\frac{g}{k} m \tag{1}
\end{equation*}
$$

The measurements are reported in the table below.

## Questions:

1- By comparing the physical equation (1) with the mathematical formula $\boldsymbol{y}=\boldsymbol{b} \boldsymbol{x}$, establish the following identifications:

$$
x=\quad, y=\quad, b=
$$

2- Complete the table below :

| i | $m_{i}(\mathbf{k g})$ | $d_{i}(\mathrm{~m})$ | $m_{i} d_{i}(\ldots)$ | $m_{i}^{2}(\ldots)$ | $b m_{i}(\ldots)$ | $\left(d_{i}-b m_{i}\right)^{2}(\ldots)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.010 | 0.03290 |  |  |  |  |
| 2 | 0.020 | 0.06650 |  |  |  |  |
| 3 | 0.040 | 0.13280 |  |  |  |  |
| 4 | 0.060 | 0.19940 |  |  |  |  |
| 5 | 0.080 | 0.26590 |  |  |  |  |
| n=.... |  |  | $\sum_{i=1}^{n} m_{i} d_{i}$ | $\sum_{i=1}^{n} m_{i}^{2}$ $=\text {. }$ |  | $\sum_{i=1}^{n}\left(d_{i}-b m_{i}\right)^{2}$ <br> = . $\qquad$ |

3- Give the numerical values of the following quantities with their corresponding units:

$$
b=\ldots . . . . . . . . . . . . . . . . . . \quad ; \quad \Delta d=\ldots . . . . . . . . . . . . \quad ; \quad \Delta b=\ldots . . . . . . . . . . . . . . .
$$

4- On the same graph sheet, represent the experimental points $\boldsymbol{d}=\boldsymbol{f}(\boldsymbol{m})$, the error bars as well as the line of slope $\boldsymbol{b}$.

5- Calculate the spring stiffness constant and put it in the form $\boldsymbol{k}=(\ldots \ldots$. ...... $\pm \ldots$......... ) .....
6- Can the repairer replace the defective spring ? Explain. We give : $\boldsymbol{g}=\mathbf{9 . 8 1} \mathbf{m} / \mathbf{s}^{\mathbf{2}}$

## PW 2 : STATIC AND DYNAMIC STUDIES OF THE OSCILLATING PENDULUM

## I. Goals :

- Highlight the movement of an elementary mechanical system: the oscillating pendulum.
- Determine the spring stiffness constant by two methods: static and dynamic.
- Measure the value of an unknown mass from the spring calibration curve.


## II. USED MATERIAL :

- A support.
- A metal rod.
- A spring of negligible mass
- A box of marked masses.
- A graduated ruler.
- A stopwatch.
- A mass of unknown value.


## III. THEORY :



## III.1. Static study:

When a mass $m$ is suspended from a spring, the latter lengthens and exerts a force $\vec{F}$ on the object responsible for its elongation; this force is called spring tension. The elongation of the spring is noted $x_{\mathrm{eq}}$ and is defined by:

$$
x_{\mathrm{eq}}=\Delta l_{0}=l-l_{0}
$$

where $\quad l_{0}:$ is the empty length of the spring
$l:$ the length of the extended spring.
A stiffness spring $k$, whose mass will be neglected, is suspended vertically by its upper end from a support.


By applying Newton's first law, we have :
At Equilibrium : $\quad \vec{P}+\vec{F}=\overrightarrow{0} \quad$ with $\quad P=m g \quad$ and $\quad F=k \Delta l_{0}=k x_{\text {eq }}$

From where, by projection on the axis of movement oriented vertically, we obtain: $P-F=0 \Rightarrow m g-k \Delta l_{0}=0$

$$
\begin{equation*}
\Rightarrow m g-k x_{\mathrm{eq}}=0 \quad \text { Thus, we have }: \quad \boldsymbol{x}_{\mathrm{eq}}=\Delta \boldsymbol{l}_{\mathbf{0}}=\boldsymbol{m} \boldsymbol{g} / \boldsymbol{k} \tag{1}
\end{equation*}
$$

## III.2. Dynamic study :

Using the previous spring, in addition to its first elongation $\Delta l_{0}=x_{\text {eq }}$ due to the clinging mass, we stretch the spring with a distance $\boldsymbol{x}$ (see the figure above).

By applying Newton's second law, we have: $\quad \vec{P}+\vec{F}=m \cdot \vec{a} \quad$ (where $\vec{a}$ is the acceleration vector) By projection on the axis of movement oriented vertically, we get : $\quad p_{x}-F_{x}=a_{x}$
Using the relations: $\quad F_{x}=k \Delta l$ with $\Delta l=\Delta l_{0}+x=x_{\mathrm{eq}}+x$
and $\quad a_{x}=\ddot{x}$, we get:

$$
\begin{aligned}
& m g-k\left(\Delta l_{0}+x\right)=m \ddot{x} \\
& m g-k\left(x_{\mathrm{eq}}+x\right)=m \ddot{x}
\end{aligned}
$$

Using the relation (1), we obtain the differential equation of the oscillatory movement.

$$
\ddot{x}+\frac{k}{m} \cdot x=0 \quad \text { with }: \quad \omega^{2}=\frac{k}{m} \quad \text { and } \quad \omega=\frac{2 \pi}{T} \quad(\omega: \text { The pulsation and } T: \text { the period })
$$

We can thus determine the expression of the period of the pendulum:

$$
\begin{equation*}
T=2 \pi \sqrt{\frac{m}{K}} \tag{2}
\end{equation*}
$$

Physically, the period $T$ represents the time of one oscillation.

## IV. EXPERIMENTAL PROCEDURE:

## IV.1. Static study:

1. Start by hanging the spring from the horizontal rod.
2. Attach the ruler so you can take precise measurements.
3. Measure the empty length $l_{0}$ of the spring.
4. Then you must first suspend the weight rack to be able to place the masses on it.
5. Different known masses $(m)$ of increasing values (see the table on the PW-sheet) are attached to the spring.

At equilibrium, measure the corresponding elongations $\left(X=x_{\text {eq }}\right)$, taking into account the mass of the weight rack.

For each mass, take a minimum of three measurements (each student will take one measurement). Record your results in the table.

## 6. To preserve the spring, you must unhook the mass directly after performing the measurement. Never leave masses attached to the spring!!

7. On a millimeter sheet, draw the calibration curve of the spring $\boldsymbol{x}_{\mathrm{eq}}=\boldsymbol{f}(\boldsymbol{m})$

## IV.2. Determination of the unknown mass of a body :

We want to determine the unknown mass $m$ of a body from the calibration curve of the spring, for this :

1. Take the device used previously and put the unknown mass to the spring.
2. Measure the elongation $\boldsymbol{x}_{\mathbf{e q}}$ of the spring.
3. Use the spring calibration curve to determine the value of the mass $m$.

## IV.3.Dynamic study :

1. Resume the previous device. Attach a known mass $m$ to the spring.
2. Stretch the spring (taking it away from its equilibrium position) a small distance $x$, perfectly vertically, then let go of the mass without initial velocity.
3. Let the mass oscillate and measure the period of the oscillations $T$ (read and carefully follow the measurement instructions on the sheet hung in the laboratory).
4. For each mass, take a minimum of three measurements (Each student will take one measurement).
5. Fill in the measurement table on the PW-sheet.
6. On a millimeter sheet, draw the calibration curve of the spring $\quad \boldsymbol{T}^{\mathbf{2}}=\boldsymbol{f}(\boldsymbol{m})$

## PW 3 : NEWTON'S LAWS

## I. GOALS :

- Study the variation of the position of a body, moving on an inclined plane, as a function of time.
- Experimental calculation of the earth's gravitational constant g.
- The calculation of the dynamic coefficient of friction $\mu_{d}$.
- The calculation of the static coefficient of friction $\mu_{s}$.


## II. USED MATERIAL :

- A carriage whose mass $m$ is labeled above.
- An inclined plane of length $L=100 \mathrm{~cm}$.
- A friction block.
- Two optical forks.
- A graduated ruler.
- A digital stopwatch


## III. THEORY :



## III.1. Movement without friction :

A carriage of mass $m$ slides on an inclined plane that makes an angle $\theta$ with the horizontal plane (see Fig.1). The fundamental principle of dynamics (FPD), neglecting the effects of plane friction, allows us to write:

$$
\vec{P}+\vec{R}=m \vec{a}
$$

$\vec{P}$ and $\vec{R}$ are weight and normal reaction forces, respectively, and $\vec{a}$ Is the acceleration vector.

The projection on the axis of movement $x$, gives us :

$$
\begin{equation*}
m g \sin (\theta)=m a \tag{1}
\end{equation*}
$$

The equation of motion of the carriage can be written in the form :

$$
x(t)=\frac{1}{2} a t^{2}+v_{0} t+x_{0}
$$

Hence, the expression of the distance $d$ traveled by this trolley, for an


Fig. 1 initial speed of zero $\left(v_{0}=0\right)$ is :

$$
\begin{equation*}
d=\frac{1}{2} a t^{2} \tag{2}
\end{equation*}
$$

## III.2. Movement with friction :

The carriage is now replaced by a friction block. This block is released, without initial speed, from the top of the inclined plane (see Fig.2). The application of FPD principle gives us:

$$
\begin{equation*}
\vec{P}+\vec{N}+\vec{f}=m \overrightarrow{a^{\prime}} \tag{3}
\end{equation*}
$$

$\vec{f}$ being the frictional force which is added in this case and $\overrightarrow{a^{\prime}}$ is the acceleration vector.

Projecting equation (3) onto the $x$ axis, we get:

$$
m g \sin (\theta)-f=m a^{\prime}
$$

with

$$
\begin{equation*}
f=\mu_{d} \cdot N \tag{4}
\end{equation*}
$$

$\mu_{d}$ is the dynamic coefficient of friction.
The projection of equation (3) on the $y$ axis, gives us:


Fig. 2

$$
\begin{equation*}
N-m g \cos (\theta)=0 \tag{5}
\end{equation*}
$$

The equation of motion of the carriage can be written in the form:

$$
x(t)=\frac{1}{2} a^{\prime} t^{2}+v_{0} t+x_{0}
$$

Hence the expression of the distance $d$ traveled by this block, for an initial speed of zero $\left(v_{0}=0\right)$ is :

$$
\begin{equation*}
d=\frac{1}{2} a^{\prime} t^{2} \tag{6}
\end{equation*}
$$

## IV. EXPERIMENTAL PROCEDURE :

## IV.1. Movement without friction :

In this part, we vary the distance between the two optical forks and we measure the time necessary for the carriage to travel this distance, taking an initial speed of zero.

1. Set the angle of inclination of the plane to $5^{\circ}$.
2. Place the carriage on the plane, so that its cursor is at the limit of the beam of the optical fork. This is the device that starts the stopwatch. If this instruction is not respected, the results will be falsified by the non-zero initial speed of the carriage when the stopwatch is started.
3. For different distances $\boldsymbol{d}$ of increasing values between the two optical forks (see the table in the TP-sheet), measure the corresponding times $t$. For each distance, take a minimum of three measurements (each student will take one measurement). When the carriage cursor crosses the beam of the second optical fork, the stopwatch stops and it displays the time elapsed for crossing this distance. Record your results in the measurement table.
4. On a millimeter sheet, draw the requested curve.

## IV.2. Movement with friction :

## IV.2.1. Determination of the dynamic coefficient of friction :

1. Consider the previously used device.
2. Set the angle of inclination of the plane to $\mathbf{2 0}^{\circ}$.
3. Replace the carriage with the friction block.
4. Put the block on the side that contains a single face of felt.
5. The block must be placed on the plane, so that its cursor is at the limit of the beam of the optical fork.
6. Drop the block with no initial velocity. Measure the duration (time) of the movement for the different distances between the two optical forks (see the table in the TP-sheet). Record your results in the measurement table.
7. On a millimeter sheet, draw the required curve.

## IV.2.2. Determination of the static coefficient of friction :

1. Take the previously used device.
2. Set the angle of inclination of the plane to $\mathbf{0}^{\circ}$.
3. Increase the angle of the incline until the block slides. Note the value of the angle.
4. Calculate the coefficient of static friction.

## V. THEORETICAL QUESTIONS (IMPORTANT) :

1. Determine the expression of the acceleration for the movement without friction (case III.1.) of the carriage $a$ depending on the earth's acceleration $g$.
2. Determine the expression of the acceleration for the movement with friction (case III.2.) of the carriage $a^{\prime}$ depending on the earth's acceleration $g$ and the dynamic coefficient of friction $\mu_{d}$.
3. Determine the expression for the static coefficient of friction $\mu_{s}$ depending on the angle of the inclined plane $\theta$.

## PW 4 : FREE FALL AND TWO-DIMENSIONAL BALLISTIC MOTION

## FIRST PART: FREE FALL

## I. GOALS :

- The study of the motion of a ball dropped without initial velocity in the gravitational field.
- The experimental determination of the acceleration of gravity $g$.
- Study of the effect of the mass on the value of the acceleration $g$.


## II. USED MATERIAL :

- Two balls of different masses.
- A vertical rod which supports at its upper end an horizontal arm.
- An electronic counter.
- A ruler graduated in millimeters.


## III. THEORY :

The relationship of distance versus time $t$ and the initial velocity of a body in free fall motion (oriented according to the $y$ axis) is given by the relation :


$$
y(t)-y_{0}=\frac{1}{2} g t^{2}+v_{0} t
$$

If we fix the origin of the heights at the starting point of the body in free fall, i.e. $y_{0}=0$ (figure above) with zero initial velocity $v_{0}=0$, the previous relation can be written in the form:

$$
y(t)=\frac{1}{2} g t^{2}
$$

## IV. EXPERIMENTAL PROCEDURE :

1. There is a vertical rod which supports at its upper end an horizontal arm.
2. At the free end of the horizontal arm, a mass $m$ is held by a trigger between the tip and the slide by which it triggers a mechanical contact.
3. As soon as the mass is released with the trigger, the mechanical contact is cut and the electronic counter starts up.
4. The mass falls in free fall on the plate which will stop the counter. This system then allows us to measure the time $t$ that the mass takes to travel a vertical distance $y$.
5. The experimental work consists in measuring the time $t$ for several vertical distances $y$. The time $t$ is taken using a digital meter.
6. For the measurement of $y$, use a ruler graduated in millimeters.
IV.1. Experience 1 : Follow the experimental procedure described above, using the ground metal ball $m_{1}$. Fill in the table found in the technical sheet.
IV.2. Experience 2 : Repeat the previous experiment using the mass plastic ball $m_{2}$.

Remarks: -The distance $y$ is measured between the lower end of the ball and the plate.
To have good measurements and for the same height, take the average of at least two time measurements.

## SECOND PART : TWO-DIMENSIONAL BALLISTIC MOTION

I. GOALS :

- The examination of a parabolic fall and the visualization of the corresponding parabolic trajectory.
- The determination of, the initial velocity of a parabolic falling projectile, the firing angle and the terrestrial acceleration $g$.
II. USED MATERIAL :
- Mini launcher
- Stainless metal ball
- pulse generator
- LED lamp

- Webcam
III. THEORY : The range is the horizontal distance, $x$, between the muzzle of the mini-shooter and the impact point of the falling ball. : $\quad \boldsymbol{x}(\boldsymbol{t})=\left(\boldsymbol{v}_{0} \cos \theta\right) \boldsymbol{t}$
where : $\quad v_{0}$ : is the initial velocity of the ball,
$\theta$ : is the angle of the horizontal inclination,
$t$ : is the flight time.
 In the vertical direction, where the force of gravity applies,
the vertical position $y(t)$ is expressed by : $\quad \boldsymbol{y}(\boldsymbol{t})=-\frac{\mathbf{1}}{\mathbf{2}} \boldsymbol{g} \boldsymbol{t}^{2}+\left(\boldsymbol{v}_{\mathbf{0}} \sin \theta\right) \boldsymbol{t}+\boldsymbol{y}_{\mathbf{0}}$.
From the equation (1), we have : $\quad t=x /\left(v_{0} \cos \theta\right)$
By taking $y_{0}=0$ and inserting equation (3) into (2), we obtain the trajectory equation:

$$
\begin{equation*}
y(x)=-\frac{g}{2 \cos ^{2} \theta v_{0}^{2}} x^{2}+(\operatorname{tg} \theta) x \tag{4}
\end{equation*}
$$

## IV. EXPERIMENTAL PROCEDURE :

1. Choose on the device (mini-launcher) the same release point (to have the same initial speed) and this by placing the ball in the mini-launcher in the first position corresponding to the first click.
2. The angle of the mini launcher is adjusted to $78^{\circ}$. It is well fixed, don't try to move it.
3. Start the pulse generator.
4. Follow the steps indicated and explained at the bench level.
5. Try to answer the questions on the technical sheet and report and calculate the quantities requested.

## PW 5 : THE SIMPLE PENDULUM

## I. GOALS :

- Highlight the movement of an elementary mechanical system: the simple pendulum.
- Study the influence of different parameters such as length and mass on the proper period of a simple pendulum.
- Visualize the oscillatory motion and calculate experimentally the value of the earth's acceleration.


## II. IMPORTANT :

- The protractor must be properly fixed to the horizontal rod to minimize errors on the angle.
- The ruler must be fixed to a nut and using the brackets located on the ruler, the length of the wire can be measured without too much difficulty.
- Reading on graduated devices such as the ruler or the protractor must be done perpendicular to the device.
- It must be ensured that the movement of the simple pendulum is indeed a swinging movement in a plane. There shouldn't be swings in all directions.


## III. USED MATERIEL :

- An adjustable foot on which a rod is fixed horizontally.
- Two balls, considered dimensionless, of masses $m_{1}$ and $m_{2}\left(m_{1} \neq m_{2}\right)$.
- A graduated ruler of length $l=1 \mathrm{~m}$.
- An inextensible wire.


## IV. THEORY :

The simple pendulum is made by suspending a ball of mass $m$ from an inextensible wire of length $l$, attached to a bracket by its upper end. The ball is moved slightly away from its equilibrium position (amplitude $\theta$ less than $10^{\circ}$ ) then released.

According to the figure opposite and by applying the fundamental principle of dynamics, we obtain :

$$
\sum \vec{F}=m \vec{a} \Rightarrow \vec{P}+\vec{T}=m \vec{a}
$$

$\vec{T}, \vec{P}$, and $\vec{a}$ represent respectively the tension of the wire, the weight of the mass suspended on the wire and the acceleration of the pendulum.

By projecting onto the tangential axis oriented towards the unitary vector $\overrightarrow{u_{r}}$, we find the equation of motion :


$$
\ddot{\theta}+\frac{g}{l} \sin \theta=0
$$

$\ddot{\theta}, l$ and $g$ represent respectively the angular acceleration of the pendulum, the length of the wire and the acceleration of earth's gravity.

Knowing that for low amplitudes, we have $\sin \theta \approx \theta$, thus we obtain :

$$
\ddot{\theta}+\frac{g}{l} \theta=0
$$

which can be written in the form :

$$
\ddot{\theta}+\omega^{2} \theta=0
$$

with $\omega^{2}=g / l$ and like $T=2 \pi / \omega$ then we get the simple period formula :

$$
T=2 \pi \sqrt{\frac{l}{g}}
$$

## V. EXPERIMENTAL PROCEDURE :

## V -1. Influence of the length $l$ of the wire on the period $T$

In this part, we try to verify the influence of the length $l$ of the wire on the period $T$ of the movement. We start by suspending the ball $m_{1}$ at the gallows, then, the length of the wire is varied. For each of the lengths considered, the ball is slightly moved away from its equilibrium position $\theta=9^{\circ}$ then it is released without initial speed. Then, we measure the period $T$ of the movement of the pendulum using the stopwatch. Finally, we draw $\boldsymbol{l}=$ $\boldsymbol{f}\left(\boldsymbol{T}^{\mathbf{2}}\right)$ on a millimeter paper.

## V -2. Influence of the mass $m$ of the pendulum on the period $T$

In this part, we want to verify the influence of the mass of the ball on the period $T$ of the movement. We replace the first mass ball $m_{1}$ by a second mass ball $m_{2}$. We do the same measurements as for the first part then we draw the graph $\boldsymbol{l}=\boldsymbol{f}\left(\boldsymbol{T}^{2}\right)$ on a millimeter paper.

